

Modeling and Optimization of Thermal Power Plant Self-Scheduling in Electricity Markets Using Quantile Regression-Based Probabilistic Price Forecasts

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Abstract:

This paper presents a comparative analysis of deterministic self-scheduling optimization for a thermal power plant under two distinct market price inputs: quantileregression-based forecasted market clearing prices and actual market clearing prices obtained from the Indian Energy Exchange (IEX). The self-scheduling problem is formulated as a Mixed-Integer Programming (MIP) model that maximizes total profit over a 24-hour scheduling horizon while satisfying technical constraints including power output bounds, ramping limits, and unit commitment logic. The model is applied to the SIPAT-I thermal generating unit in the Indian grid and implemented in GAMS, solved with CPLEX. Results reveal that forecasted high-price scenarios yield significantly higher profits (Rs. 116,942,000) compared to actual market conditions (Rs. 35,818,000), with the actual-price case exhibiting operational losses during off-peak hours due to prices falling below marginal costs. The study underscores the critical impact of price forecast accuracy on self-scheduling decisions and operational profitability.

Key Terms— Self-scheduling, Unit commitment, Mixedinteger programming, Quantile regression, Market clearing price, GAMS, Thermal power plant, Indian Energy Exchange.

I. Introduction

The deregulation of electricity markets has transformed the operating environment for power producers, granting them autonomy to make self-scheduling decisions that optimize profit rather than following centrally dispatched schedules [1]. In competitive electricity markets, a generating unit's profitability is intimately tied to the accuracy of price forecasts and the scheduling strategy adopted in response to anticipated market conditions.

The self-scheduling problem involves determining the on/off commitment status and power output level of a generating unit over a planning horizon—typically 24 hours—with the objective of maximizing profit while respecting operational constraints such as ramping limits and minimum/maximum generation bounds [?]. The

problem is inherently combinatorial due to binary commitment variables and is formulated as a Mixed-Integer Linear Program (MILP).

A central challenge in self-scheduling is that market clearing prices (MCPs) are unknown at the time of decision-making. Two broad strategies are commonly employed: (i)

deterministic scheduling using a single forecasted price trajectory, and (ii) stochastic scheduling that hedges across multiple price scenarios. Price forecasting methods range from statistical time-series models to machine learning approaches; quantile regression has gained traction for capturing price uncertainty by providing distributional forecasts [2].

This paper focuses on the deterministic framework applied under two price inputs:

- Case 1: Forecasted MCPs derived from quantile regression, representing an optimistic high-price scenario.

- Case 2: Actual MCPs recorded from the Indian Energy Exchange (IEX) for the same 24-hour period, reflecting real market volatility.

By comparing outcomes under these two inputs, this study quantifies the performance gap attributable to price forecast error and provides insight into the operational and financial implications of scheduling under imperfect price information.

The remainder of the paper is organized as follows. Section II presents the mathematical formulation of the self-scheduling model. Section III describes the case system data. Section IV reports and analyzes computational results for both cases. Section V provides a comparative discussion, and Section VI concludes the paper.

II. Problem Formulation

A. Objective Function

The self-scheduling problem for a single thermal generating unit maximizes total profit Π over the 24-hour horizon $T = \{1, 2, \dots, 24\}$:

$$\max \Pi = \sum_{t \in T} \pi(t) \tag{1}$$

where the profit per period $\pi(t)$ is:

$$\pi(t) = \lambda(t)p(t) - C_v p(t) - C_f v(t) - C_{su} y(t) - C_{sd} z(t) \tag{2}$$

The terms represent, respectively, energy revenue, variable generation cost, fixed operating cost, start-up cost, and shut-down cost. Variable definitions are provided in Table I.

B. Power Output Limits

When the unit is online ($v(t) = 1$), its output must lie between minimum stable generation and rated capacity:

| | |
|-----------|------------------------------------|
| $\pi(t)$ | Profit at period t (Rs.) |
| C_v | Variable (marginal) cost (Rs./kWh) |
| C_f | Fixed operating cost (Rs./h) |
| C_{su} | Start-up cost (Rs.) |
| C_{sd} | Shut-down cost (Rs.) |
| P_{max} | Maximum generation capacity (MW) |
| P_{min} | Minimum stable generation (MW) |
| R_U | Ramp-up rate limit (MW/h) |
| R_D | Ramp-down rate limit (MW/h) |
| RSU | Start-up ramp limit (MW) |
| RSD | Shut-down ramp limit (MW) |
| v_0 | Initial commitment status |
| p_0 | Initial power output (MW) |

$$P_{min} v(t) \leq p(t) \leq P_{max} v(t), \forall t \in T \tag{3}$$

C. Ramping Constraints

Ramp-up constraint for $t > 1$:

$$p(t) - p(t-1) \leq R_U v(t-1) + RSU y(t) + P_{max}(1 - v(t)) \tag{4}$$

Ramp-up constraint for $t = 1$ (using initial conditions):

$$p(1) - p_0 \leq R_U v_0 + RSU y(1) + P_{max}(1 - v(1)) \tag{5}$$

Ramp-down constraint for $t > 1$:

$$p(t-1) - p(t) \leq R_D v(t) + RSD z(t) + P_{max}(1 - v(t-1)) \tag{6}$$

Ramp-down constraint for $t = 1$:

$$p_0 - p(1) \leq R_D v(1) + RSD z(1) + P_{max}(1 - v_0) \tag{7}$$

D. Unit Commitment Logic Constraints

The relationship between commitment status, start-up, and shut-down indicators for $t > 1$:

$$y(t) - z(t) = v(t) - v(t-1), \forall t > 1 \tag{8}$$

For $t = 1$:

$$y(1) - z(1) = v(1) - v_0 \tag{9}$$

Mutual exclusion of start-up and shut-down events:

$$y(t) + z(t) \leq 1, \forall t \in T \tag{10}$$

TABLE I: Nomenclature

| Symbol | Description |
|--------------|---|
| $\lambda(t)$ | Market clearing price at period t (Rs./kWh) |
| $p(t)$ | Power output at period t (MW) |
| $v(t)$ | Binary: 1 if unit is online, 0 otherwise |
| $y(t)$ | Binary start-up indicator |
| $z(t)$ | Binary shut-down indicator |

TABLE II: SIPAT-I Unit Technical and Economic Parameters

| Parameter | Symbol | Value |
|----------------------|-----------|----------|
| Maximum capacity | P_{max} | 1,980 MW |
| Minimum power output | P_{min} | 100 MW |
| Ramp-up limit | R_U | 90 MW/h |
| Ramp-down limit | R_D | 80 MW/h |
| Start-up ramp limit | RSU | 300 MW |

| | | |
|--------------------------|----------|--------------|
| Shut-down ramp limit | RSD | 200 MW |
| Fixed cost | C_f | Rs. 1.32/h |
| Variable (marginal) cost | C_v | Rs. 1.40/kWh |
| Start-up cost | C_{su} | Rs. 20 |
| Shut-down cost | C_{sd} | Rs. 10 |
| Initial status | v_0 | 0 (offline) |
| Initial power output | p_0 | 0 MW |

E. Variable Domains

$$v(t), y(t), z(t) \in \{0,1\}, \forall t \in T \tag{11}$$

$$p(t) \geq 0, \forall t \in T \tag{12}$$

The complete model (1)–(10) constitutes a Mixed Integer Linear Program (MILP), implemented in GAMS and solved with CPLEX with optcr = 0 (optimality gap tolerance of zero).

III. Case System Data

A. Generating Unit Parameters

The model is applied to the SIPAT-I thermal generating unit, a coal-fired plant connected to the Indian grid. Technical and economic parameters are listed in Table II.

B. Price Input Scenarios

Quantile Regression (QR) Price Forecasting: Unlike Ordinary Least Squares (OLS), which estimates the conditional mean, Quantile Regression estimates a specific conditional quantile $\tau \in (0,1)$ of the response variable. This is particularly useful in electricity markets to model price spikes and skewness.

Mathematical Formulation: The QR model solves the following optimization problem for the coefficients β :

$$\min_{\beta} \sum_{i=1}^n \rho_{\tau}(y_i - x_i^T \beta) \tag{13}$$

The check function $\rho_{\tau}(u)$ is an asymmetric loss function defined as:

$$\rho_{\tau}(u) = \begin{cases} \tau u, & u \geq 0 \\ (\tau - 1)u, & u < 0 \end{cases} \tag{14}$$

By varying τ (e.g., 0.1,0.5,0.9), the model provides lower, median, and upper price forecasts, offering

robustness against outliers and capturing extreme price behaviors.

TABLE III: Hourly Market Clearing Prices – Both Cases (Rs./kWh)

| Period | Case 1 | Case 2 | Period | Case 1 | Case 2 |
|--------|--------|--------|--------|--------|--------|
| t1 | 4.14 | 3.96 | t13 | 1.81 | 0.12 |
| t2 | 3.81 | 3.63 | t14 | 1.79 | 0.15 |
| t3 | 3.52 | 3.57 | t15 | 2.19 | 0.30 |
| t4 | 3.47 | 3.57 | t16 | 2.67 | 0.59 |
| t5 | 3.40 | 3.52 | t17 | 2.98 | 1.46 |
| t6 | 3.57 | 3.90 | t18 | 3.43 | 2.84 |
| t7 | 3.73 | 4.09 | t19 | 5.07 | 3.56 |
| t8 | 3.21 | 3.06 | t20 | 10.00 | 4.76 |
| t9 | 2.71 | 1.62 | t21 | 10.00 | 4.40 |
| t10 | 2.34 | 0.67 | t22 | 10.00 | 4.05 |
| t11 | 1.86 | 0.27 | t23 | 10.00 | 4.17 |
| t12 | 1.80 | 0.20 | t24 | 9.94 | 3.75 |

1) Case 1 – Forecasted Prices (Quantile Regression): Hourly price forecasts for the scheduling day were generated using quantile regression on historical IEX market clearing prices. The median quantile trajectory was selected as the deterministic price input. The forecasted prices range from Rs. 1.79/kWh (t14) to Rs. 10.00/kWh (t20–t23), with a pronounced evening price peak characteristic of Indian power markets during high-demand periods. Full hourly prices are listed in Table III.

Fig. 1: Hourly Market Clearing Prices – Case 1 vs Case 2

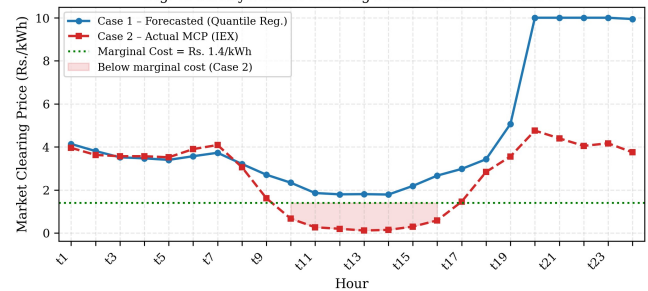


Fig. 1: Price profiles with marginal cost line below-cost shading.

2) Case 2 – Actual Market Clearing Prices: The actual MCPs recorded on the IEX for the same day are used as the price input. These prices range from Rs. 0.12/kWh (t13) to Rs. 4.76/kWh (t20), displaying a significantly different profile: very low off-peak prices during hours t10–t16 (below marginal cost) and a moderate evening peak. This case tests the scheduling strategy under real market price realizations.

IV. Computational Results

The MILP model contains 169 single equations, 121 single variables (72 binary), and 620 non-zero elements. Both cases reached proven optimality with zero absolute gap.

A. Case 1: Forecasted High Prices

1) Commitment and Dispatch: The optimal solution commits the unit for all 24 hours ($v(t) = 1, \forall t$). At $t = 1$, the unit starts up ($y(1) = 1$) at 300 MW—constrained by the start-up ramp limit ($R_{su} = 300$ MW). Output then increases by exactly $R_U = 90$ MW per hour through t_1 – t_{19} , ramping from 300 MW to 1,920 MW. Maximum capacity (1,980 MW) is reached at t_{20} and maintained through t_{24} .

2) Financial Performance: Period profits $\pi(t)$ are positive throughout, ranging from Rs. 514.68 (t_{12}) to Rs. 17,026.68 (t_{20} – t_{23}). The exceptional profitability during the evening peak (t_{20} – t_{23} , price = Rs. 10.00/kWh, output = 1,980 MW) drives the outstanding total profit. Key financial metrics are:

- Total profit: Rs. 116,942,020 (\approx Rs. 11.69 Crores)
- Average hourly profit: Rs. 4,872,584
- Operating hours: 24/24
- Peak hourly profit (t_{20} – t_{23}): Rs. 17,026.68 per period

3) Binding Constraints: Ramp-up constraints are binding for periods t_2 through t_{19} , confirming that ramping limits—not price economics—govern the output trajectory during the build-up phase. The capacity constraint ($p \leq P_{max}$) becomes binding at t_{20} – t_{23} where the shadow price is Rs. 8.60/MW, indicating significant value of additional capacity during peak hours.

B. Case 2: Actual Market Clearing Prices

1) Commitment and Dispatch: The unit remains online for all 24 hours, again starting up at t_1 with $y(1) = 1$. The power output profile follows a similar ramp-up pattern but with a notable deviation at t_{10} : output drops from 1,020 MW (t_9) to 990 MW (t_{10}), breaking the monotonic ramp due to the very low price at that hour (Rs. 0.67/kWh). After t_{10} , ramping resumes until the unit reaches 1,980 MW at t_{21} – t_{24} .

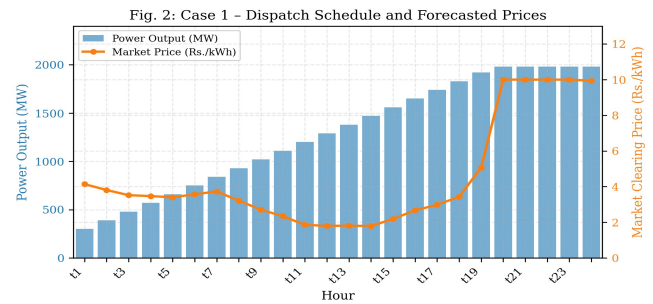


Fig. 2: Case 1 dispatch — market price .

2) Financial Performance: In stark contrast to Case 1, period profits turn negative during hours t_{10} – t_{16} due to market prices falling well below the marginal cost ($C_v =$ Rs. 1.40/kWh). Losses peak at -Rs. 1,688.82 at t_{14} (price = Rs. 0.15/kWh). Despite these interim losses, continuous operation is optimal because shutting down would incur start-up/shut-down costs and forfeit profitable evening periods. Key financial metrics are:

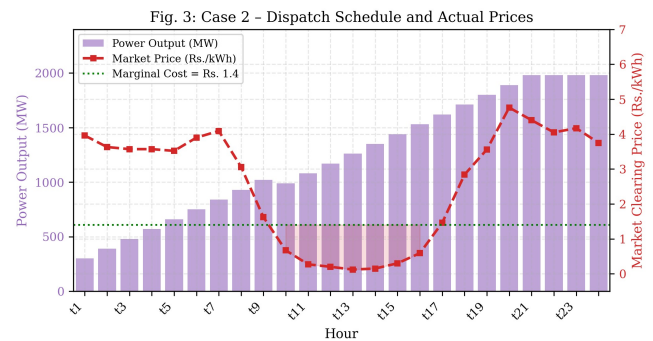


Fig. 3: Case 2 dispatch — market price .

- Total profit: Rs. 35,818,420 (\approx Rs. 3.58 Crores)
- Average hourly profit: Rs. 1,492,434
- Operating hours: 24/24
- Loss-making periods: t_{10} – t_{16} (7 hours)
- Peak hourly profit (t_{20}): Rs. 6,349.08
- Worst hourly profit (t_{14}): -Rs. 1,688.82

3) Binding Constraints: Ramp-up constraints are binding for t_2 – t_9 and t_{11} – t_{21} . The capacity constraint binds only at t_{21} – t_{24} , with smaller shadow prices (Rs. 2.35– 2.77/MW) reflecting the more moderate peak prices in Case 2. The marginal value of the ramp-up constraint at t_2 is Rs. 15.76, significantly lower than Case 1 (Rs. 28.16), consistent with lower price levels.

C. Hourly Results Summary

Table IV presents the complete hourly dispatch and profit for both cases.

V. Comparative Discussion

A. Profit Gap and Price Forecast Impact

The forecasted-price case (Case 1) achieves a total profit of Rs. 116,942,020, while the actual-price case (Case 2) yields Rs. 35,818,420—a reduction of 69.4%. This large gap is attributable primarily to three factors:

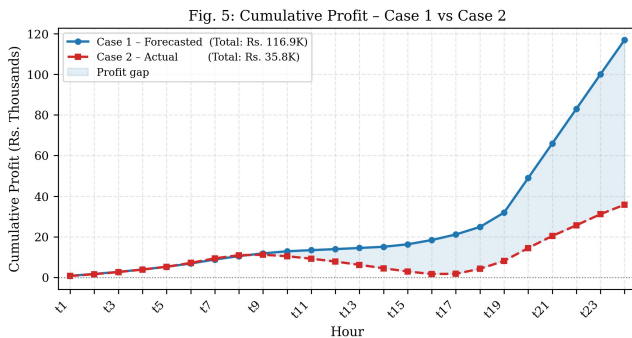


Fig. 4: Cumulative profit with gap shading (Rs. 116,942,020 vs 35,818,420).

TABLE IV: Hourly Optimal Dispatch Results – Cases 1 and 2

| [Rs.] | Case 1 (Forecasted) | | Case 2 (Actual) t | |
|-------|---------------------|----------------|-------------------|-----------|
| | $p(t)$ [MW] | $\pi(t)$ [Rs.] | $p(t)$ [MW] | $\pi(t)$ |
| 1 | 300 | 800.68 | 300 | 746.68 |
| 2 | 390 | 938.58 | 390 | 868.38 |
| 3 | 480 | 1,016.28 | 480 | 1,040.28 |
| 4 | 570 | 1,178.58 | 570 | 1,235.58 |
| 5 | 660 | 1,318.68 | 660 | 1,397.88 |
| 6 | 750 | 1,626.18 | 750 | 1,873.68 |
| 7 | 840 | 1,955.88 | 840 | 2,258.28 |
| 8 | 930 | 1,681.98 | 930 | 1,542.48 |
| 9 | 1020 | 1,334.88 | 1020 | 223.08 |
| 10 | 1110 | 1,042.08 | 990 | -724.02 |
| 11 | 1200 | 550.68 | 1080 | -1,221.72 |
| 12 | 1290 | 514.68 | 1170 | -1,405.32 |
| 13 | 1380 | 564.48 | 1260 | -1,614.12 |
| 14 | 1470 | 571.98 | 1350 | -1,688.82 |
| 15 | 1560 | 1,231.08 | 1440 | -1,585.32 |
| 16 | 1650 | 2,094.18 | 1530 | -1,240.62 |
| 17 | 1740 | 2,747.88 | 1620 | 95.88 |
| 18 | 1830 | 3,713.58 | 1710 | 2,461.08 |
| 19 | 1920 | 7,045.08 | 1800 | 3,886.68 |
| 20 | 1980 | 17,026.68 | 1890 | 6,349.08 |
| 21 | 1980 | 17,026.68 | 1980 | 5,938.68 |
| 22 | 1980 | 17,026.68 | 1980 | 5,245.68 |
| 23 | 1980 | 17,026.68 | 1980 | 5,483.28 |
| 24 | 1980 | 16,907.88 | 1980 | 4,651.68 |
| Total | | 116,942.02 | | 35,818.42 |

1) Peak price magnitude: Forecasted prices during t20–t23 reached Rs. 10.00/kWh versus Rs. 4.05– 4.76/kWh actual, a 2.1× overestimate. The contribution of peak-hour

revenue to total profit is disproportionately large at maximum capacity.

2) Off-peak price accuracy: Case 1 prices during t10– t16 (Rs. 1.79–2.34/kWh) remained above marginal cost, so all periods were profitable. Case 2 prices in the same window collapsed to Rs. 0.12–0.67/kWh, producing 7 loss-making periods.

3) Ramping trajectory: Despite the output dip at t10 in Case 2, both cases operate at full capacity during peak hours. The profit differential is therefore a direct consequence of price level, not dispatch volume.

B. Operational Strategy Comparison

Both cases result in the unit staying online for all 24 hours. This outcome is rational: the start-up cost (Rs. 20) and shut-down cost (Rs. 10) are small relative to the opportunity cost of being offline during the profitable evening peak. Even when per-period losses are incurred (Case 2, t10–t16), the aggregate loss (Rs. 7,279.90) is less than the transition costs plus foregone evening profit that would result from shutting down and restarting.

C. Constraint Activity

Ramp-up constraints are the primary binding operational constraints in both cases, reflecting that the unit’s

TABLE V: Comparative Performance Metrics

| Metric | Case 1 | Case 2 |
|---------------------------|-------------|-------------|
| Total profit (Rs.) | 116,942,020 | 35,818,420 |
| Total profit (Rs. Crores) | 11.69 | 3.58 |
| Operating hours | 24/24 | 24/24 |
| Loss-making periods | 0 | 7 (t10–t16) |
| Max hourly profit (Rs.) | 17,026.68 | 6,349.08 |
| Min hourly profit (Rs.) | 514.68 | -1,688.82 |
| Peak power output (MW) | 1,980 | 1,980 |
| Hours at full capacity | 5 (t20–t24) | 4 (t21–t24) |
| Price range (Rs./kWh) | 1.79–10.00 | 0.12–4.76 |
| Profit gap vs. Case 1 | – | -69.4% |
| CPLEX solve time (s) | 0.047 | 0.047 |
| MIP iterations | 109 | 169 |

90 MW/h ramp rate is the limiting factor during the buildup phase. The shadow price of the ramp-up constraint is consistently higher in Case 1 (range Rs. 3.67–30.90/MW) compared to Case 2 (range Rs. 0.22–18.32/MW), confirming that

ramping capacity has greater economic value under higher price environments.

D. Performance Metrics Summary

Table V summarizes the key performance indicators for both cases.

VI. Conclusion

This paper presented a detailed comparative analysis of deterministic self-scheduling optimization for the SIPATI thermal unit under quantile-regression-based forecasted prices (Case 1) and actual IEX market clearing prices (Case 2). Both cases were solved to global optimality using GAMS/CPLEX.

Key conclusions are:

- 1) The forecasted high-price scenario achieves a total profit of Rs. 116.94 million, demonstrating the maximum achievable profitability when price forecasts accurately capture evening price peaks.
- 2) The actual-price case yields Rs. 35.82 million—a 69.4% reduction—with 7 loss-making periods during off-peak hours, highlighting the sensitivity of self-scheduling outcomes to price forecast accuracy.
- 3) In both cases, continuous 24-hour operation is optimal. The ramp-up rate is the binding physical constraint during the generation build-up phase, motivating the value of higher ramp-rate units in volatile price environments.
- 4) The shadow prices of ramp-up constraints are substantially higher under forecasted prices, confirming that ramping flexibility commands greater economic value when prices are elevated.
- 5) Price forecast accuracy—particularly for peak-hour prices—is the dominant determinant of realized profit in deterministic self-scheduling. Overestimated peak prices by quantile regression create inflated profit expectations compared to actual market outcomes.

These findings motivate the use of stochastic or robust optimization frameworks that hedge across multiple price scenarios, reducing the exposure to forecast errors while maintaining acceptable expected profitability.

Acknowledgment

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